

**FINITE ELEMENT METHODS**  
**(Mechanical Engineering)**

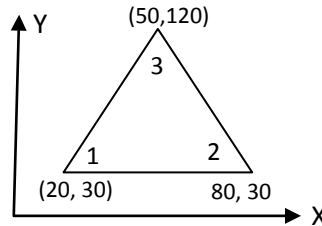
Time: 3 hours

Max. Marks: 70

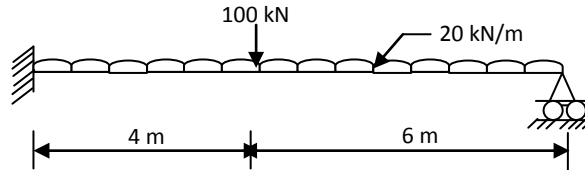
Answer any FIVE questions  
All questions carry equal marks

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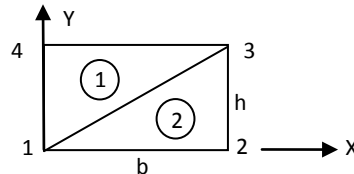
- 1 (a) Is there any connection between the FEM and the boundary element method (BEM)?  
(b) Explain the stress-strain relation.  
) (c) Draw a typical three dimensional element and indicate state of stress in their positive senses.
- 2 Evaluate the stiffness matrix for the elements shown in figure below. The coordinates are given in units of millimeters. Assume plane stress conditions. Let  $E = 210$  GPa, passion ratio 0.25, and thickness 10 mm:



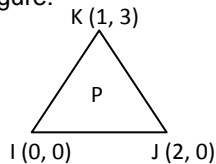
- 3 Determine the consistent nodal vector due to loads acting on the beam shown in figure:



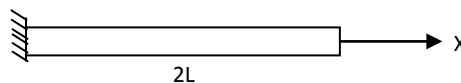
- 4 Compute the stiffness matrix of element 1 of the two-triangle element model of the rectangular plate in plane stress shown in figure. Then use it to compute the stiffness matrix of element 2.



- 5 (a) Using natural coordinates derive the shape function for a linear quadrilateral element.  
(b) Write short notes on:  
(i) Uniqueness of mapping of isoparametric elements. (ii) Gaussian quadrature integration technique.
- 6 Find the temperature at a point  $P(1, 1.5)$  inside a triangular element shown with nodal temperatures given as  $T_i = 40^\circ\text{C}$ ,  $T_j = 34^\circ\text{C}$  and  $T_k = 46^\circ\text{C}$ . Also determine the location of the  $42^\circ\text{C}$  contour line for the triangular element shown in figure:



- 7 Explain the Flowchart of two-dimensional fluid-flow process.
- 8 Determine the first two natural frequencies, for the bar shown in figure, with length  $2L$ , modulus of elasticity  $E$ , mass density  $\rho$ , and cross-sectional area  $A$ ,



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